In the Final Analysis

The 2006 L S Theobald Lecture

delivered at the University of Plymouth on 03/05/06 by

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The three essentials of quality

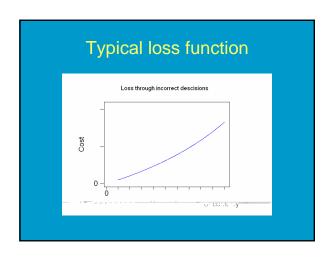
- What accuracy does the customer <u>NEED</u>?
 Fitness for purpose (Decision theory)
- What accuracy <u>CAN</u> I achieve? Single laboratory validation Collaborative trials
- What accuracy <u>DO</u> I achieve? Internal quality control Proficiency testing

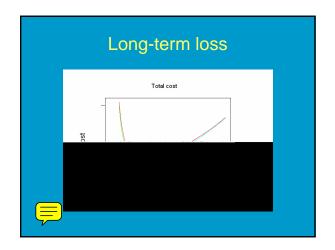
Three issues relating to quality

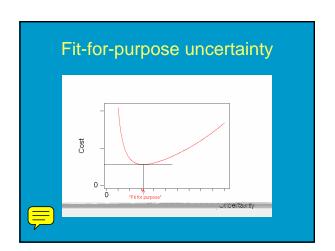
- Fitness for purpose (What is it?)
- Statistics (Can we do it?)
- Metrology (Do we need it?)

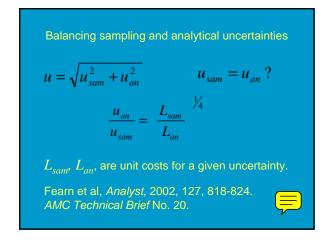


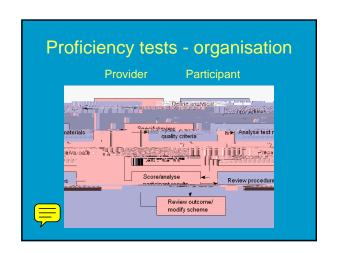


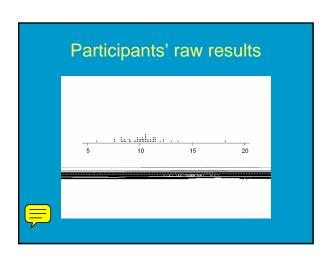


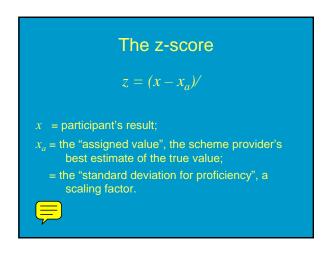


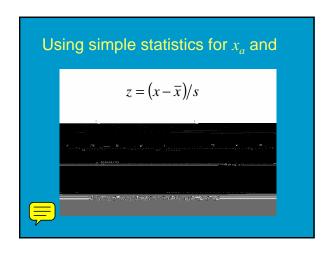


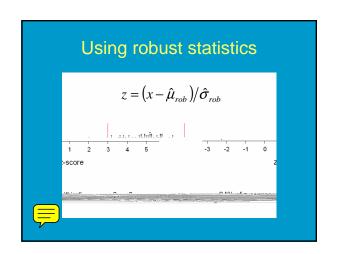


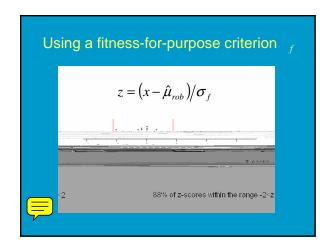




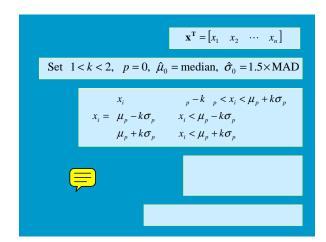








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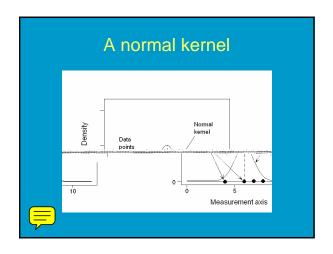


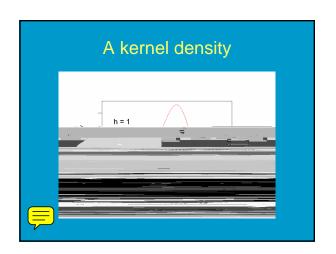


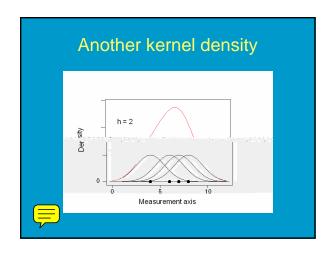


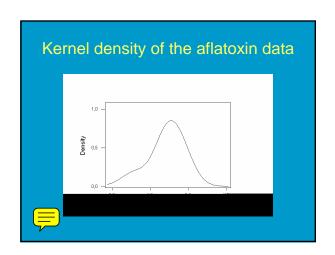


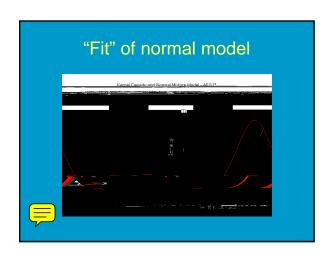
The normal kernel density $y = \frac{1}{nh} \sum_{i=1}^{n} \Phi \ \frac{x - x_i}{h}$ where is the standard normal density, $\Phi(a) = \frac{\exp(-a^2/2)}{\sqrt{2\pi}}$ AMC Technical Brief No. 4











The normal mixture model

$$f(y) = \sum_{j=1}^{m} p_j f_j(y), \quad \sum_{j=1}^{m} p_j = 1$$

$$f_j(y) = \frac{\exp(-(y - \mu_j)^2 / 2\sigma^2)}{\sqrt{2\pi}\sigma}$$

AMC Technical Brief No 23, and AMC Software. Thompson, Acc Qual Assur, 2006, 10, 501-505.

Mixture models found by the maximum likelihood method (the EM algorithm)

• The M-step

$$\hat{p}_{j} = \sum_{i=1}^{n} \hat{P}(j|y_{i}) / n$$

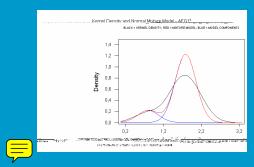
$$\hat{\mu}_{j} = \sum_{i=1}^{n} y_{i} \hat{P}(j|y_{i}) / \sum_{i=1}^{n} \hat{P}(j|y_{i})$$

$$\hat{\sigma}^{2} = \sum_{j=1}^{n} \sum_{i=1}^{m} ((y_{i} - \hat{\mu}_{j})^{2} \hat{P}(j|y_{i})) / \hat{P}(j|y_{i})$$

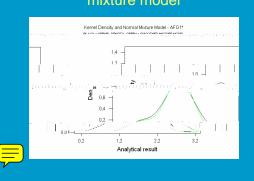
• The E-step
$$\hat{P}(j\big|y_i) = \hat{p}_j f_j(y_i) \bigg/ \sum_{j=1}^m \hat{p}_j f_j\left(y_i\right)$$



Kernel density and fit of 2-component normal mixture model



Kernel density and variance-inflated mixture model



Find out more?

AMC Technical Briefs and Software on www.rsc.org/amc/

Statistics

· Lies, damned lies, and statistics!

Metrology

• Fiction, science fiction, and metrology!

Metrologist's creed

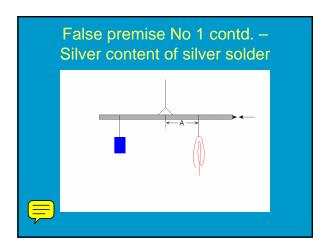
- Uncertainty is important.
- Analytical chemists are not good at estimating uncertainty.
- All results of chemical measurement are traceable to SI units, in particular the mole, the kilogramme, the metre.
- Analytical chemists don't worry about traceability, that's why their results are questionable.

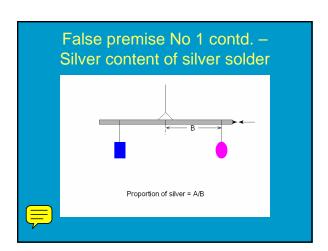


Metrological false premise 1

- All analytical results are traceable to SI units, in particular the mole, the kilogramme, and the metre
- NO! The majority of analytical measuremnts made for commercial purposes are mass fractions, not traceable to any unit.
 Corollory: expressions such as %, ppm, ppb, etc are perfectly correct.







False premise No 1 contd. – Silly or what!

- Is the concentration of silver, A/B, traceable to the metre?
- Should we express the result as (say) 70 cm m⁻¹?
- Or 700 mg g⁻¹ (when no mass standard is involved)?



Metrological false premise 2

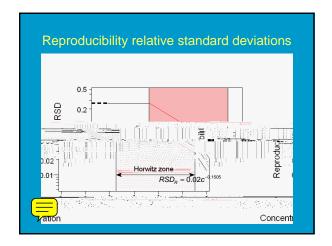
- Chemical measurement results are not accurate enough, and that is because of a lack of traceability to SI units.
- NO! Most chemical measurement results are fit for purpose or more accurate.
- Where results are not accurate enough—it sometimes happens—the shortfall is often irreducible and traceability to SI units does not help

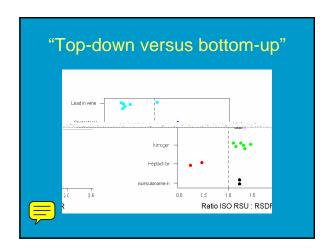


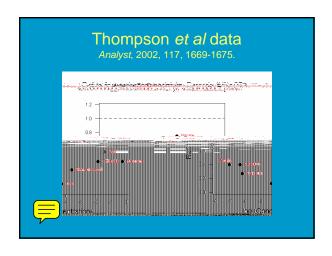
Metrological false premise 3

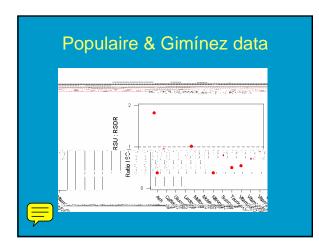
- Uncertainty is under-estimated by interlaboratory studies: only "bottom-up" models with clear traceability to SI units give the correct answer.
- NO! When proper comparisons are made, we mostly find that (say) reproducibility standard deviations from collaborative trials give equal or greater uncertainty estimates than "bottom-up".











Metrological false premise 4

- Chemical measurements have a larger relative uncertainty in comparison with most physical measurements. (True)
- That is because they are not traceable to SI units.
- NO! The traceability chain to SI units contributes almost nothing to the combined uncertainty of analytical results.

Metrological false premise 4 contd.

- Realistic relative uncertainties in analytical results are mostly in the approximate range 1-30%.
- Relative uncertainties in transerring SI units (such as mass and volume) to the analytical laboratory bench are less than 0.1%.

Metrological false premise 5

- Terms such as "true value", "trueness", and "bias" have no proper place in metrology (because we can't know them).
- NO! "True value" (and its dependent terms) are readily defined.
- The whole of statistics is based on the idea of unknown population values, a concept logically isomorphic with "true value".

Metrological false premise 6

- Only accredited laboratories can produce reliable results.
- <u>No!</u> Evidence from proficiency tests contradicts this idea.



Metrological false premise 6 Difference between means =0.008 % m/m (0.8 standard errors) Accredited Not accredited 2.5 2.6 2.7 2.8 2.9 3.0 Result, Nitrogen in meat, % m/m

